# Chapter 4: measures of dispersions IQV

1) Measure of dispersion in qualitative variables.

|                         | IQV | Variance | St.d. |
|-------------------------|-----|----------|-------|
| Nominal variable        | Yes | No       | No    |
| Ordinal variable        | Yes | No       | No    |
| Interval/ratio variable | Yes | Yes      | Yes   |

2) What is IQV (Index of Qualitative Variations/variables)

$$IQV = \frac{K(100^2 - \sum Pct^2)}{100^2(K-1)}$$
 K: total number of groups; Pct: percentage of each group

#### 3) Example

|           | Fayetteville AR 2020 |  |
|-----------|----------------------|--|
| White     | 74%                  |  |
| Black     | 6%                   |  |
| Asian     | 3%                   |  |
| Hispanics | 9%                   |  |
| Others    | 8%                   |  |
| IQVs      | 54%                  |  |

$$IQV = \frac{K(100^2 - \sum Pct^2)}{100^2(K - 1)}$$

$$IQV = \frac{5 \times (10000 - (74^2 + 6^2 + 3^2 + 9^2 + 8^2))}{10000 \times 4} = 54\%$$

#### 4) Interpretations

$$0 \le IQV \le 1 \ or \ 100\%$$

When IQV is close to 0, it means the group dispersion is minimum, when IQV is close to 1 or 100%, it means the group dispersion is great.

For example, in terms of racial composition, if IQV is 80%, compared with IQV being 20%. The former means the racial diversity if very high, whereas the latter means the racial diversity is low.

### 5) Exercise

|           | Fayetteville AR 2020 | Fayetteville AR 2000 |
|-----------|----------------------|----------------------|
| White     | 74%                  | 84%                  |
| Black     | 6%                   | 5%                   |
| Asian     | 3%                   | 3%                   |
| Hispanics | 9%                   | 5%                   |
| Others    | 8%                   | 3%                   |
| IQVs      | 54%                  | 36%                  |

$$IQV = \frac{K(100^2 - \sum Pct^2)}{100^2(K - 1)}$$

## 6) IQV computations with numbers not percentages

|           | Fayetteville AR 2020 | Springdale AR 2020 |
|-----------|----------------------|--------------------|
| White     | 74%                  | 34,543             |
| Black     | 6%                   | 1,733              |
| Asian     | 3%                   | 1,791              |
| Hispanics | 9%                   | 33,287             |
| Others    | 8%                   | 12,807             |
| Total Pop | 100%                 | 84,161             |
| IQVs      | 54%                  | 81%                |