Chapter 3: measures of central tendency in frequency table

1) What is central tendency measure?

Central tendency is what average case look like
Average income by occupation, by region, by race/gender, average height, weight, etc.
2) Mode

Mode: is the group in a variable with the highest frequency

| Gender | Frequency | percentage | proportion |
| :--- | :--- | :--- | :--- |
| Men | 7 | $7 / 26 * 100$ <br> $=26.9 \%$ | $7 / 26=.27$ |
| Women | 19 | $19 / 26=$ <br> 73.1 | $19 / 26=.73$ |
| N (total number of cases) | 26 | 100 | 1.00 |

Mode for gender for our class is "women."
3) Median

Median is the middle point splitting the sample into two equal halves.

If N is odd number; the median would be located at the $\left(\frac{N+1}{2}\right)^{t h}$ location in a sample that is ascending ordered.

For example, if $N=9$, then the median would be $(9+1) / 2=5^{\text {th }}$.

If $N$ is an even number, the median would be the average between the two values in $\left(\frac{N}{2}\right)^{\text {th }}$ and $\left(\frac{N}{2}+1\right)^{\text {th }}$ location in a sample that is ascending ordered.

| age | frequency | Cumulative <br> frequency |
| :--- | :--- | :--- |
| 12 | 42 | 42 |
| 23 | 12 | 54 |
| 32 | 32 | 86 |
| 41 | 19 | 105 |
| 55 | 58 | 163 |
| 60 | 37 | 200 |
| 75 | 5 | 205 |
| N | 205 | --- |

The median would be located at $(206) / 2=103^{\text {rd }}$
The median $=41$
4) mean
$\bar{X}=\frac{\sum X_{i} \times F_{i}}{N}$

| age | frequency | Cumulative <br> frequency |
| :--- | :--- | :--- |
| 12 | 42 | 42 |
| 23 | 12 | 54 |
| 32 | 32 | 86 |
| 41 | 19 | 105 |
| 55 | 58 | 163 |
| 60 | 37 | 200 |
| 75 | 5 | 205 |
| N | 205 | --- |

$\bar{X}=\frac{12 \times 42+23 \times 12+32 \times 32+41 \times 19+55 \times 58+60 \times 37+75 \times 5}{205}$
$\bar{X}=40.8$

For this sample, the median is 41 , and the mean is 40.8 , so it is left skewed.
5) properties of central tendency measures
median is not sensitive to the outliers, whereas the mean is very sensitive to the outliers

| Case \# | Sample A | Sample B |
| :--- | :--- | :--- |
| 1 | $\$ 45 \mathrm{~K}$ | $\$ 45 \mathrm{~K}$ |
| 2 | $\$ 55 \mathrm{~K}$ | $\$ 55 \mathrm{~K}$ |
| 3 | $\$ 60 \mathrm{~K}$ | $\$ 60 \mathrm{~K}$ |


| 4 | $\$ 78 \mathrm{~K}$ | $\$ 78 \mathrm{~K}$ |
| :--- | :--- | :--- |
| 5 | $\$ 90 \mathrm{~K}$ | $\$ 150,000 \mathrm{~K}$ |
| Median | $\$ 60 \mathrm{~K}$ | $\$ 60 \mathrm{~K}$ |
| Mean | $\$ 65.6 \mathrm{~K}$ | $\$ 30,048 \mathrm{~K}$ |



This is right skewed graph because mean is on the right side of median (Mean > Median)
6) exercise, for the following frequency table, please compute its mode, median and mean

| Age | frequency | Cumulative <br> frequency |
| :--- | :--- | :--- |
| 1 | 142 | 142 |
| 9 | 1 | 143 |
| 30 | 320 | 463 |
| 49 | 190 | 653 |
| 51 | 58 | 711 |
| 67 | 137 | 848 |
| N | 848 | --- |

Mode $=30$
Median $=30 ; 848 / 2=424^{\text {th }}$, and $425^{\text {th }} ;$
Mean $=36.8$
7) when to use which

|  | mode | median | Mean |
| :--- | :--- | :--- | :--- |
| Nominal | Yes | No | No |
| Ordinal | Yes | No | No |
| Interval/ratio | Yes | Yes | Yes |

